# JacobiNeRF: NeRF Shaping with Mutual Information Gradients







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## **Preview: Plain NeRF Lacks Semantic Awareness**





(a) random neurons



(b) a single layer



(c) a block of layers

"Jiggling" the neuron weights of the NeRF results in diffuse perturbations that are not semantically aligned



images

(a)

(b)

(c)





## **Preview: User Interactions with 3D Scenes through 2D Views**







#### selecting

editing





#### label propagation



## **Preview: Encode Semantic Correlations into a NeRF**









## **Preview: NeRF Shaping with Mutual Information Gradients**









## **Preview: Label Propagation**





Semantic Seg

Instance Seg





#### Example sparse annotation interaction



## **User Interactions with NeRFs**







## Semantic Structure of a Scene is Reflected in its Co-Variations





#### this chair has moved



the table became longer



#### the table became darker





## **Mutual Information and 2nd Order Relationships**



A is more correlated with B than with C  $\mathbb{I}(\mathsf{A},\,\mathsf{B}) > \mathbb{I}(\mathsf{A},\,\mathsf{C})$ X is more correlated with Y than with Z  $\mathbb{I}(\mathsf{X},\,\mathsf{Y}) > \mathbb{I}(\mathsf{X},\,\mathsf{Z})$ 



## **Shaping Neural Representations**

## Can we shape NeRFs to better reflect mutual correlations in the scene?

The scene tangent space









 $\mathbb{I}(\mathsf{A},\mathsf{B}) > \mathbb{I}(\mathsf{A},\mathsf{C})$  $\mathbb{I}(X,Y) > \mathbb{I}(X,Z)$ 



## Mutual Information via NeRF Gradients



Mutual information

$$\mathbb{I}(\hat{I}(\mathbf{p}_i), \hat{I}(\mathbf{p}_j)) \approx \left| \cos\left(\frac{\partial \Phi_i}{\partial \theta^D}, \frac{\partial \Phi_j}{\partial \theta^D}\right) \right|$$

Inter-pixel correlations are captured by cosine similarity of the NeRF Jacobians

$$I(\mathbf{p}_i) = \Phi(\mathbf{o}_i, \mathbf{v}_i; \theta)$$
  

$$I(\mathbf{p}_j) = \Phi(\mathbf{o}_j, \mathbf{v}_j; \theta)$$
  

$$\hat{I}(\mathbf{p}_i) = \Phi(\mathbf{o}_i, \mathbf{v}_i; \theta^D + \mathbf{n})$$
  

$$\hat{I}(\mathbf{p}_j) = \Phi(\mathbf{o}_j, \mathbf{v}_j; \theta^D + \mathbf{n})$$



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## Setting up Semantic "Neuronal Resonances" via Aligning Gradients





Shaping co-aligns gradients of correlated points (here points of the same semantic class)



## **NeRF MLP Shaping via Mutual Information Gradients**



## General purpose image feature: DINO

**Obtain some source of semantic affinity** 



InfoNCE contrastive loss on gradients + reconstruction loss

Contrastive training aligning gradients



## NeRF Shaping Causes Gradient Alignment





## **Application: Editing Appearance**













## **Application: Editing Appearance**













## **Application: Entity Selection**

#### image











#### NeRF

#### JacobiNeRF





From a single point we can select an entire semantic entity.





## **Application: Label Propagation**

## Acquire dense labels of a scene given sparse annotations.



## Label one pixel for each class from one view





#### Dense label for any view



## **Propagation Through Resonances**

## 2D version (JacobiNeRF-2D)

#### Given m labels



Source view

Perturb along gradients



**Target view** 



#### m responses

.....



## Semantic Segmentation (sparse 1pix/class, Replica)





Given label



#### J-NeRF 3D





## Semantic Segmentation (sparse 1pix/class, Replica)





## Semantic Segmentation (sparse 1pix/class, Replica)

#### 1 pix/class 1 view 30 28.3 26.3 25 25.3 20 18.7 18.1 15 Semantic NeRF DINO NeRF 3D J-NeRF 2D DINO 2D J-NeRF 3D

#### mloU

Average results on 7 scenes, 180 test views for each scene



Acc



## Semantic Segmentation (dense 1view, Replica)



Given label





#### J-NeRF 3D





## Semantic Segmentation (dense 1view, Replica)









## Semantic Segmentation (dense 1view, Replica)

#### Dense label 1 view



#### mloU

Average results on 7 scenes, 180 test views for each scene





Acc



## Instance segmentation (sparse, 1pix/instance, ScanNet)

Source View



#### Target View

GT





## Instance segmentation (sparse, 1pix/instance, ScanNet)



#### mloU

Average results on 4 scenes, ~180 test views for each scene

#### Acc



## Instance segmentation (1 view, dense, ScanNet)

### Source view Target view GT



# DINO-2DD-NeRFJ-NeRF 3DImage: Dino-2DImage: Dino-2DImage:



## Instance segmentation (1 view, dense, ScanNet)



#### mloU

Average results on 4 scenes, ~180 test views for each scene

#### Acc





#### https://github.com/xxm19/jacobinerf



